

1 **Using stacked SDMs with accuracy and rarity weighting to optimize surveys for**  
2 **rare plant species**

3  
4 \*Hanna Rosner-Katz, Department of Biology Carleton University

5 Department of Biology, Carleton University 1125 Colonel By Drive, Ottawa ON K1S 5B6

6 Jenny L. McCune, Ph.D., Department of Biology Carleton University

7 Department of Biology, Carleton University 1125 Colonel By Drive, Ottawa ON K1S 5B6

8 Current address: Department of Biological Sciences, University of Lethbridge, 4401

9 University Drive, Lethbridge AB T1K 3M4

10 Joseph R. Bennett, Ph.D., Department of Biology Carleton University

11 Department of Biology, Carleton University 1125 Colonel By Drive, Ottawa ON K1S 5B6

12 \*Corresponding author: [hanna.rosner.katz@glel.carleton.ca](mailto:hanna.rosner.katz@glel.carleton.ca)

13 **ABSTRACT**

14 Effective conservation of rare species requires reasonable knowledge of population  
15 locations. However, surveys for rare species can be time-intensive and therefore  
16 expensive. We test a methodology using stacked species distribution models (S-SDMs)  
17 to efficiently discover the greatest number of new rare species' occurrences possible.  
18 We used S-SDMs for 22 rare plant species in southern Ontario, Canada to predict the  
19 best survey locations among individual 1-ha cells. For each cell, we weighted  
20 distribution model outputs by accuracy and species rarity to create an efficiency value.  
21 We used these efficiency values as an index to determine the locations of our field  
22 surveys. We conducted field surveys in multi-species cells, "MSC" (areas with high  
23 predicted efficiency for multiple species) and single species cells, "SSC" (areas with  
24 high probability for only one species) to determine the relative efficiency of a multi-

25 species survey approach. MSC were more than twice as likely as SSC to have at least  
26 one rare plant species discovered. Efficiency ranks were also useful in directing  
27 surveyors toward incidental discoveries of other rare species that were not modeled.  
28 Our technique of using S-SDMs can help direct surveys to more efficiently find rare  
29 species occurrences.

30 **Key-words:** prioritization, Maxent, forest plants, model accuracy, conservation status

## 31 **1. Introduction**

32 To effectively monitor and protect rare species, we must know the geographic  
33 locations of their populations, but many rare species lack precise distribution  
34 information. Field surveys are needed to fill these gaps (Peterson et al. 2011), but they  
35 are time-consuming and expensive (Lindenmayer et al. 2013). Thus, reliable protocols  
36 are needed to help efficiently direct survey efforts.

37 Species distribution models have recently proliferated as conservation tools  
38 (Guisan et al. 2013). By using species occurrence data along with environmental or  
39 spatial predictors, the habitat suitability or probability of occurrence for a species can be  
40 predicted across an area of interest (Guisan & Zimmerman 2000, Elith et al. 2006).  
41 SDMs have also been used to predict current species richness (e.g. Guisan & Theurillat  
42 2000, Newbold et al. 2009, Parvianen et al. 2009), predict future species richness with  
43 changing climate (Thuiller et al. 2005), predict shifts in species' distributions (e.g.  
44 Thuiller 2004, Elith et al. 2010, McKenney et al. 2014), assess the efficacy of current  
45 protected areas and propose locations for new ones (Loiselle et al. 2003, Koch et al.  
46 2017, Amaral et al. 2017), prescribe management for invasive species (Bennett 2014),

47 and find new occurrences of rare species (e.g. Williams et al. 2009, Rebelo & Jones  
48 2010, Peterson et al. 2011, McCune 2016).

49         Outputs of SDMs for individual species can be stacked together to create one  
50 composite map (Ferrier & Guisan 2006); this technique is often referred to as S-SDM  
51 (where the “S” stands for stacking; Dubuis et al. 2011). S-SDMs offer an effective  
52 method for highlighting areas of special conservation importance based on predictions  
53 of species richness of a taxonomic group of interest (Newbold et al. 2009, Yu et al.  
54 2017), and have been used to predict threatened species richness (Parvianen et al.  
55 2009; Koch et al. 2017). Knowledge of which areas have the highest potential  
56 concentration of rare species can point to promising survey sites, thus leading to the  
57 discovery of previously unknown rare species locations (Williams et al. 2009). This in  
58 turn increases the accuracy of the estimate of the number of rare species populations,  
59 which allows for a more accurate assessment of a species’ conservation status and  
60 better-informed management.

61         Two aspects that have begun to receive attention in the S-SDM literature are: 1)  
62 accuracy of SDMs, and 2) species’ conservation status. The accuracy of distribution  
63 models for individual species (not stacked) has been discussed extensively (e.g.  
64 Segurado & Araaujo 2004, Elith & Leathwick 2009). A model that overpredicts suitable  
65 habitat and makes commission errors will waste survey resources by sending surveyors  
66 to unsuitable areas that were predicted to be suitable, while a model that underpredicts  
67 suitable habitat and makes omission errors will cause surveyors to overlook areas  
68 where the species is present (Loiselle 2003). Stacking individuals models together in a  
69 S-SDM can lead to inaccurate predictions in the form of species richness (usually, but

70 not always, as an overestimation, Guisan and Rahbek 2011), for which correction  
71 methods have been proposed (Calabrese et al. 2014, Del Toro et al. 2019, Pouteau et  
72 al. 2015). Fewer studies have accounted for individual model accuracy, within the  
73 resulting S-SDMs (but see Dunn et al. 2016). When working within an S-SDM  
74 framework, there will be variation in the accuracy of the individual models being stacked  
75 due to the differing characteristics of the species being modeled (Guisan et al. 2007,  
76 Syphard & Franklin 2010), the quality of the data for each species (e.g. Graham et al.  
77 2004, Moudrý & Šímová 2012,), and the relative prevalence of the species (Hernandez  
78 et al. 2006, Le Lay et al. 2010). Fernandes et al. 2018 examined the effects on the  
79 predictive accuracy of S-SDMs for virtual species by varying individual model  
80 components known to affect accuracy at the single model level and found that sampling  
81 size and modeling technique had the largest impacts. However, we have yet to see  
82 individual SDM accuracy for real species quantitatively estimated based on data  
83 independent of the records used to build the SDM, rigorously evaluated, and weighted  
84 within the S-SDM framework itself. In fact, assessing the accuracy of SDMs using  
85 independently collected presence and absence data is rarely done in any context. It is  
86 important to take individual model accuracy into account in the stacking process if the  
87 goal is to focus on survey locations with the highest probabilities of containing at least  
88 one of the species of interest, as would be the case in attempts at rare species  
89 discovery.

90         Secondly, many agencies prioritize management of species based on rarity (e.g.  
91 ESA 1973; SARA 2002), so knowing where less prevalent species are may be more  
92 important than knowing where more prevalent species are. Some modelers have noted

93 this fact and have weighted individual models in S-SDMs by species' relative rarity  
94 (Albuquerque & Beier 2016, Tukainen et al. 2017, Yu et al. 2017), or have used the  
95 habitat specificity of the species (Miličić et al. 2017) to highlight potential areas  
96 important for threatened species conservation. However, to our knowledge, no study  
97 has tested whether weighting individual model outputs by both rarity and accuracy  
98 within an S-SDM framework leads to an increased detection rate of priority threatened  
99 and rare species.

100 To do so, we built SDMs for 22 rare vascular plant species in southern Ontario,  
101 Canada and stacked them, weighting each individual model by accuracy, species  
102 conservation status, both, or neither. This weighting procedure allowed us to create an  
103 index based on the resulting efficiency values, from which we conducted field surveys in  
104 areas predicted to be suitable for one or more species to test the effectiveness of these  
105 S-SDM maps in leading to the discovery of new rare plant occurrences. We aimed to  
106 test i) How much more likely are surveys to lead to the discovery of at least one rare  
107 species in cells with high predicted probability of occurrence for multiple rare species,  
108 compared to cells with high predicted probability of occurrence for only one species (i.e.  
109 how much do we gain in survey efficiency by stacking SDMs), and ii) What effect does  
110 weighting individual species' models by model accuracy and/or species rarity have on  
111 survey efficiency?

## 112 **2. Methods**

### 113 2.1 Study Region and Species

114 We focused our study on the forests of Southern Ontario (Figure 1),  
115 predominantly in the Carolinian forest zone of the extreme southwest (Crins et al. 2009),  
116 which is characterized by deciduous canopy cover. We also located some study sites in  
117 the forests north and east of the Carolinian zone, which are characterized by mixed  
118 deciduous-evergreen cover (Crins et al. 2009). Southern Ontario is important for  
119 vascular plants at both the provincial and national level, as approximately 72% of  
120 Ontario's and more than 40% of Canada's plant species occur here (Oldham 2017),  
121 despite the dominance of urban development and agricultural land use (Crins et al.  
122 2009). The total study area encompasses approximately 7 million hectares.

123 We initially selected 27 vascular plant species native to Ontario and growing in  
124 woodland habitats, based on their conservation importance, and their relative ease of  
125 identification in the field. We defined rare species as those ranked S1, S2, or S3 at the  
126 provincial level, corresponding to critically imperiled, imperiled, and vulnerable species  
127 (Faber-Langendoen et al. 2012, Table 1). Most of the species included here are at the  
128 northern edge of their range within southern Ontario, with large portions of their ranges  
129 extending south into the United States. The species represent a wide taxonomic range  
130 and include trees, shrubs, herbs and ferns. Nomenclature follows the Ontario Natural  
131 Heritage Information Centre (NHIC, [https://www.ontario.ca/page/get-natural-heritage-](https://www.ontario.ca/page/get-natural-heritage-information)  
132 [information](https://www.ontario.ca/page/get-natural-heritage-information)).

## 133 2.2 Building and Evaluating Individual Models

134 We obtained presence-only occurrence records for each species from the NHIC.  
135 These records include herbarium records, field surveys by Ministry of Natural  
136 Resources (MNR) biologists, and other confirmed sightings. We used only records that

137 had <100 m accuracy to build the SDMs, to correspond with the resolution of the  
138 environmental variables (see below). The total number of occurrence records we used  
139 to build the models ranged from 4 to 1594 with a mean of 83.7 records per species and  
140 a median of 17.5 (Table 1). Species with occurrence records on the lower end of this  
141 range are potentially subject to overfitting (Merow et al. 2013); however, SDMs can  
142 perform well even with sample sizes as low as 5 (Hernandez et al. 2006; Pearson et al.  
143 2007, van Proosdij et al. 2016) and we are specifically studying rare species with limited  
144 available records. Additionally, species that have lower prevalence (i.e. percent area  
145 occupied within the study region) require fewer records than higher prevalence species  
146 to achieve similar model accuracy (van Proosdij et al. 2016). In the case of most of the  
147 species we modeled here, they can reasonably be assumed to have low prevalence  
148 within our study region given the infrequency of sightings (see results for further  
149 validation of this assumption). Records date from 1897 to 2012. We considered high  
150 spatial accuracy to be the most important criterion for including occurrence records.  
151 However, we explored the effect of record age on the performance of SDMs and found  
152 minimal effect on model accuracy when using records with <100 m spatial accuracy  
153 (unpublished data). While we only used the partial range for each species in their  
154 respective SDMs (the study region as opposed to their entire extent of occurrence), our  
155 study region represents the edge of the range for most species included here, which  
156 has been found to produce more accurate model results than including the complete  
157 range (Luoto et al. 2005). Because we evaluated each SDM prior to including it in the S-  
158 SDM based on independently collected presence and absence records, we are able to  
159 exclude SDMs that had low accuracy as a result of few occurrence records, sampling

160 bias in the records, or any of the many other factors that can influence SDM accuracy  
161 (see Merow et al. 2013).

162 We collected data on climatic, topographic, soil, and surficial geology  
163 environmental variables to use as predictors in the models (Online Resource 1).  
164 Previous research (McCune 2016) suggests that forest type and the amount of forest on  
165 the landscape surrounding a site can influence whether a threatened plant species is  
166 present. Therefore, we also collected data on forest contiguity (number of 1-hectare  
167 cells out of the 9x9 cell area immediately surrounding the focal cell that are forested)  
168 and land cover type (deciduous forest, mixed forest, swamp, etc.) across the study  
169 region. We tested for multicollinearity between environmental predictors and used only  
170 those that were not highly correlated ( $r < 0.7$ ), following Gogol-Prokurat (2011). Where 2  
171 variables were correlated at  $r > 0.7$ , the more generalized variable was used (e.g., mean  
172 annual temperature and mean temperature of the warmest quarter were correlated so  
173 the former was kept). We resampled each variable to a 100m x 100m resolution using  
174 the Resample function in ArcGIS and the “Majority” resampling technique (see Online  
175 Resource 1 for original spatial resolutions for each variable)

176 Because the occurrence data were presence-only records and were limited in  
177 number, we chose to use Maxent (Phillips et al. 2006) to build SDMs. Maxent has been  
178 shown to perform very well using a range of performance measures (Elith & Graham  
179 2009), even when few species occurrence records are available (Hernandez et al. 2006,  
180 Pearson et al. 2007, van Proosdij et al. 2016). We built 8 different SDMs for each  
181 species (Figure 2). As a beginning foundation, all models for each species contained  
182 the climatic, topographic, soil, and surficial geology predictor variables (14 predictors).

183 Additionally, we built models that included either the forest contiguity or land cover  
184 variables or both to determine if these less commonly used variables would help  
185 improve the accuracy of models for any species. We ran each of these model types  
186 twice: once with a regularization multiplier set to 1 and once with regularization set to  
187 0.5. The regularization parameter can correct for model overfitting, with higher values  
188 allowing for a more generous inclusion of predicted suitable habitat and lower values  
189 providing a more conservative estimate of predicted suitable habitat. Given the desire to  
190 narrow down the area for potential survey sites as much as possible, we chose to test a  
191 lower regularization parameter value in addition to the default value of 1. Testing  
192 different regularization parameters is recommended, in order to arrive at the best-  
193 performing model (Merow et al. 2013). We set aside a random subsample of 25% of  
194 available records to test each model and fit the model 10 times with different model  
195 fitting and test subsamples, making the final result an average of the outputs from the  
196 subsamples. We used Maxent's cumulative output in which each grid cell receives a  
197 score from 0 to 100, which can be interpreted as the percentage of cells that have a  
198 value equal to or less than that cell's value (Merow et al. 2013). We set features in  
199 Maxent to auto (which includes linear, quadratic, product, threshold, and hinge  
200 functions), jackknife to measure variable important was selected, and set the  
201 background as the complete study area. We set the random test percentage to twenty-  
202 five percent with replicated run type of subsample.

203 We evaluated the models with independent presence and absence data  
204 originating from two sources. First, we obtained independent presences from the  
205 NHIC's central holdings database, which consists of records that have not yet been

206 added to the main database of occurrences. Second, we obtained independent  
207 presences and absences from 2014 and 2015 field data in which botanists surveyed  
208 156 100m x 100m cells throughout Southern Ontario predicted to be suitable for one or  
209 more rare plant species (see McCune 2016; McCune et al. 2017). We excluded any  
210 independent presence located within the same grid cell as a record used to build the  
211 SDM, using the raster package in R (R Core Team 2016, Hijmans & van Etten 2017).  
212 We also excluded absences if the grid cell was surveyed outside the time of year during  
213 which the plant is present and identifiable.

214 We chose one SDM for each species based on three criteria: 1) first, we chose  
215 the model with the highest sensitivity (the percent of actual presences correctly  
216 classified as presences by the model) based on calculations with the independent data  
217 (i.e. the model that predicted the highest number of independent presence records as  
218 suitable) using a threshold that achieved 10% omission of training presences for  
219 species with at least 15 records, and 0% omission (i.e. threshold = minimum training  
220 presence suitability) for species with fewer than 15 records.; 2) if more than one model  
221 was tied for the highest sensitivity, we chose the model with the highest AUC (a  
222 threshold independent measure of model performance, Fielding & Bell 1997); 3) if there  
223 was still a tie between models, we chose the model with the lowest area predicted  
224 suitable (Engler et al. 2004). We considered sensitivity to be the most important  
225 measure of predictive performance for this study because we wanted to minimize the  
226 number of false negatives produced by each model. If an area is falsely characterized  
227 as unsuitable, then it will not be surveyed and rare occurrences will be missed as a  
228 result of omission error (Liu et al. 2016). We used a 0% omission rate for species with

229 very few occurrences because with fewer known occurrences, it is less likely that the  
230 lowest 10% suitability values represent areas unsuitable for the species; this approach  
231 is recommended by Pearson et al. (2007). We chose model AUC as a selection factor  
232 because of its independence from a threshold, its ubiquitous use by modelers, and its  
233 generally effective measure of model discrimination ability (e.g. Pearce & Ferrier 2000).  
234 Smallest suitable area was also used as a selection factor because narrowing down the  
235 area considered suitable for a species narrows down the potential survey area, an  
236 important consideration when time is a limiting factor.

237         It is important to recognize that the MaxEnt predicted habitat suitability does not  
238 necessarily correlate linearly with species probability of occurrence (Gogol-Prokurat  
239 2011, Vaughan & Ormerod 2005). Therefore, we converted MaxEnt suitability outputs  
240 from the best SDM for each species (which range from values of 0 to 100) to estimated  
241 probabilities of occurrence (0 to 1 value range) based on the independent presence and  
242 absence data described above, using generalized linear models (GLMs) with a binomial  
243 link function. Gogol-Prokurat (2011) tested for a linear relationship between SDM output  
244 and probability of occurrence using a modified Hosmer-Lemeshow deciles of risk test.  
245 However, we recognize that these relationships may be significant but not linear, so we  
246 used binomial GLMs. We extracted Maxent suitability values for each presence and  
247 absence location, using the suitability values as the explanatory factor in the logistic  
248 model. We used the resulting GLMs to create new rasters for each species in which  
249 each cell represents the probability of occurrence of that species in that cell. This  
250 allowed us to estimate the likelihood of species presence in a cell based on  
251 independent data not used to build the SDM. To test the usefulness of the GLM for

252 predicting species probability of occurrence, we compared it to an intercept-only model  
253 and deemed habitat suitability a significant predictor of probability of occurrence when  
254  $\Delta AIC$  was less than 2 (Burnham & Anderson, 2002).

### 255 2.3 S-SDM Efficiency Maps

256 We used only the species that had acceptable AUC values and GLM probability  
257 of occurrence models that were significantly better than an intercept-only model ( $\Delta AIC >$   
258 2; Burnham & Anderson 2002) in the stacking process, to avoid using models that were  
259 not useful for predicting species distributions. We defined acceptable AUC values as  
260 those  $\geq 0.6$  since an AUC value of 0.5 is no better than random. Although a common  
261 practice is to consider AUC values  $\geq 0.7$  as adequate (Swets 1988), we adopted 0.6 as  
262 the cutoff because the species modeled here are rare, and we assumed that any  
263 information that is better than random is potentially important for creating useful models  
264 that could be used in management. Additionally, evaluating the models with  
265 independently collected data from field surveys (as opposed to data separated from the  
266 original dataset) further helped to ensure all models included in the stack produced  
267 reasonable results.

268 To create the efficiency maps, we stacked the estimated probability of occurrence  
269 model outputs for these 22 species in four ways: 1) individual estimated probability of  
270 occurrence maps added together with no weighting; 2) probabilities of occurrence  
271 added together and weighted by accuracy of the SDM (as measured by AUC) and by  
272 the S-rank (threat level) of the species, using the following equation:

$$273 \quad (1) E_i = \sum_{j=1}^n (P_{ij} \cdot R_j \cdot A_j)$$

274 Where  $E_i$  is the resulting Efficiency Index of cell  $i$ ,  $P_{ij}$  is the estimated probability of  
275 occurrence of species  $j$  occurring in cell  $i$ ,  $R_j$  is the rarity weight (i.e., provincial S-rank  
276 where  $S_1=3$ ,  $S_2=2$ ,  $S_3=1$ ) of species  $j$ , and  $A_j$  is the accuracy of the SDM for species  $j$   
277 as measured by AUC ; 3) models weighted by accuracy but not by rarity; and 4) models  
278 weighted by rarity but not by accuracy. We used a rarity weighting because rarer  
279 species are of greater priority and urgency for locating new populations. We used an  
280 accuracy weighting because when field survey time is limited, it is best to visit areas  
281 with greater confidence in the model predicting the species' probability of occurrence.

## 282 2.4 Field Surveys

283 We selected candidate cells for surveys that were either highly suitable for  
284 multiple species or suitable for just one species. We term the former multi-species cells  
285 (MSC) and the latter single-species cells (SSC). There has been some debate about the  
286 appropriateness of applying a suitability threshold and obtaining binary predicted  
287 presence/absence maps for individual species (bS-SDM) compared to using raw  
288 estimated probability of occurrence values (pS-SDM) (Guisan & Rahbek 2011,  
289 Calabrese et al. 2014, D'Amen et al. 2015); we used both methods in identifying MSC  
290 and SSC. Specifically, we defined MSC as being suitable for 2 or more species using a  
291 threshold allowing for a 10% omission rate for species with greater than 15 records  
292 used to build their SDM, and a 0% omission rate for species with fewer than 15 records  
293 (bS-SDM), while also having an efficiency index within the top 5% of all grid cells  
294 according to the s-SDM weighted by both accuracy and rarity (pS-SDM) (Parviainen et  
295 al. 2009). These two constraints taken together ensured that cells were not chosen for  
296 surveys that had low to moderate probability of species presence for many species. We

297 defined SSC as being suitable for only one species (using the same omission rate  
298 threshold rules as defined above) independent of the cell's efficiency value. We  
299 attempted to survey the same number of MSC and SSC within each tertiary level  
300 watershed (subdivisions of secondary watersheds which are mostly made up of large  
301 river systems) to reduce spatial segregation of MSC and SSC. On each survey day, we  
302 randomly chose several cells among the possible MSC/SSC within a given watershed  
303 and surveyed the first site for which we could obtain landowner permission. Because of  
304 the limited amount of time available to conduct these searches, both in our study and  
305 commonly in practice by field botanists, we did not survey sites with low habitat  
306 suitability for all species. These sites are unlikely to harbor any of our modeled species,  
307 and the goal of our study was to test the efficiency of S-SDMs versus single SDMs to  
308 direct surveys for rare species. Thus, these would not have been useful to survey.

309         We surveyed 70 cells (including 33 MSC and 37 SSC) on privately owned sites  
310 as well as protected areas (e.g. Nature Conservancy of Canada, Nature Trust, or  
311 Provincial Park land), between May and August 2017. We obtained written or verbal  
312 permission from the landowners for all privately owned sites, and research permits for  
313 protected areas. At each site, we navigated to the center of the 100m by 100m grid cell  
314 using a handheld GPS unit and used flagging tape and a compass to delineate four  
315 quadrants. The field team included one to four people with at least one trained botanist  
316 present. We walked the entire square grid cell systematically, recording all vascular  
317 plant species observed. Each survey lasted 2.5-5 hours.

## 318 2.5 Comparison of S-SDM Methods

319 We built logistic regression models to test the significance of the relationship  
320 between the efficiency values (four versions for each surveyed cell) and the probability  
321 of finding any rare plant species at that location based on our field surveys. We also  
322 tested for differences between MSC and SSC in the total, native, and exotic species  
323 richness recorded, using t-tests assuming unequal variances. We performed all data  
324 analysis in R 3.3.1 (R Foundation for Statistical Computing, Vienna, Austria 2016).

### 325 **3. Results**

326 The independent AUC value for the best MaxEnt models for each species ranged  
327 from 0.442 to 0.999 with a mean of 0.83 (Online Resource 2). Five species were  
328 excluded from further analysis due to low model accuracy: three based on low  
329 independent AUC values and two based on  $\Delta AIC < 2$  (Burnham & Anderson 2002)  
330 when comparing their GLMs to an intercept-only model. This left 22 species included in  
331 the S-SDM efficiency maps.

332 Of the 70 cells surveyed, 22 had at least one rare plant species (ranked S1, S2,  
333 or S3). Fifteen had one species, five plots had 2, and two plots had 3. We found a total  
334 of 30 occurrences of 17 rare plant species. Only 4 out of these 17 species were those  
335 we modeled and incorporated into the efficiency maps (*Castanea dentata*, *Celtis*  
336 *tenuifolia*, *Cornus florida*, and *Lithospermum latifolium*), the rest being incidental  
337 discoveries of species not modeled by the SDMs (Online Resource 3).

338 The probability of finding at least one rare plant species was approximately  
339 double in MSC compared to SSC. Including incidental rare plant discoveries, MSC had  
340 a 42.4% success rate (presence of at least one rare species) while the SSC had a

341 21.6% success rate. Not including the incidental species, the MSC had an 18.2%  
342 success rate while the SSC had an 8.1% success rate (Figure 3). Results were  
343 qualitatively the same when excluding SSC sites where we had no paired MSC. None of  
344 the measures of species richness (total, native, or exotic) were significantly different  
345 between the two site types.

346 GLMs relating the estimated probability of occurrence of at least one rare plant  
347 species to the efficiency index showed little difference among weighting procedures  
348 used to create the S-SDMs. All  $\Delta AIC$  values were  $<5$  and percent deviance explained  
349 by the full models was similar (Table 2). There was a significant positive relationship in  
350 the logistic regression between the efficiency index values of all the S-SDMs and the  
351 probability of at least one rare species (target and incidental species included) being  
352 present ( $p = 0.01$ ). Results were similar when only target species were included. There  
353 was no significant relationship between the calculated efficiency index values and the  
354 field-measured total species richness ( $p = 0.21$ ,  $R^2 = 0.01$ ) or total species richness and  
355 estimated probability of occurrence of a rare species ( $p = 0.23$ ).

#### 356 **4. Discussion**

357 The efficiency maps we created by stacking the probability of occurrence model  
358 outputs for 22 rare plant species allowed for the discovery of new occurrences of 17  
359 rare species. These discoveries were approximately twice as likely to occur in multi-  
360 species (MSC) sites, where multiple species were predicted to have suitable habitat,  
361 than in single-species (SSC) sites, where only one species was predicted to have  
362 suitable habitat. While we found new occurrences of only 4 out of the 22 species  
363 modeled, because we were working with rare species this discovery rate is not unusual

364 (MacDougall & Loo 2002, Williams et al. 2009, McCune 2016). Our results point to the  
365 usefulness of pairing modeling with field surveys for uncovering previously unknown  
366 rare species occurrences, thereby increasing our knowledge of rare species  
367 distributions and habitat occupancy.

368         We found 11 rare plant species which were not modeled and not incorporated  
369 into the efficiency maps. This preponderance of incidental finds suggests that the  
370 efficiency index not only helps to find species explicitly modeled, but also those which  
371 are not modeled but also rare. Thus, the efficiency index is capturing something shared  
372 in the ecological niches of the species modeled as well as in some rare species that  
373 were not modeled. We noticed that the incidental rare species that we discovered tend  
374 to prefer mesic, moderately shaded, floodplain conditions in older woodlands.  
375 Therefore, our efficiency index may be especially helpful at highlighting these areas for  
376 surveys.

377         The most important variables included in the individual models according to  
378 percent contribution were surficial geology, land cover, and soil texture. The most  
379 important variables according to permutation importance (Online Resource 4) were  
380 annual mean temperature, precipitation of the warmest quarter, forest contiguity, and  
381 mean temperature of the growing season. It seems that these environmental variables  
382 largely dictate the presence or absence of rare species in our study area. The  
383 importance of the land cover variable to the performance of the majority of the models is  
384 of particular note given the unresolved question of its inclusion as an appropriate and  
385 useful predictor in SDMs; of especial concern can be its categorical (rather than  
386 continuous) nature and its resolution size in relation to species' scale of interaction with

387 their environments (Bucklin et al. 2015, Cord et al. 2014, Eskildsen et al. 2013, Wilson  
388 et al. 2013). Our results agree with those of Pearson et al. (2004), who found that  
389 adding land cover to their distribution models for plant species improved predictive  
390 performance. Additionally, the results of Luoto et al. (2007) showed increased model  
391 accuracy including land cover as a predictor when spatial resolution was fine. These  
392 results also agree with those of this study given the high resolution of our variables and  
393 resulting cells within the models. It may be possible to even further improve model  
394 accuracy with the addition of continuous remote sensing predictors (Cord et al. 2014),  
395 however the good to excellent performance of most of our models indicates that a  
396 categorical land cover variable may be sufficient, especially for rare species that prefer  
397 distinct land cover type(s). We are not surprised that land cover was important for  
398 many of our modeled species, as it likely allowed MaxEnt to focus on areas of the  
399 proper forest type (coniferous, mixed, or deciduous) and remove areas of agricultural or  
400 urban land use.

401         The efficiency index performed better at predicting rare species presence than a  
402 simple measure of total species richness: there was no significant relationship between  
403 total species richness and probability of rare species presence in the logistic regression,  
404 while there was a significant positive relationship between the efficiency index and rare  
405 species probability of presence (Figure 3b). This is important because, at least for rare  
406 plants in our study region, creating SDMs for a subset of rare species may be sufficient  
407 if the main goal is to locate new rare species sharing a given habitat type., rather than  
408 creating models to predict total species richness, which may require more information.

409           It must be noted that this efficiency index will not be useful for finding new rare  
410 plant species occurrences in every situation. Firstly, the efficiency index did not result in  
411 the discovery of any species ranked S1, those which are the most imperiled in the  
412 province. This is likely because these species are the least prevalent and thus any new  
413 population locations (if they exist) will be the most difficult to find. Le Lay et al. (2010)  
414 had similar results when attempting to discover new occurrences of two extremely rare  
415 plant species based on ensembles of SDMs.

416           Secondly, the efficiency index will not aid in the discovery of rare species that  
417 have very distinct habitat requirements and thus are not likely to occur in the MSC of  
418 our efficiency maps. The MSC represent areas that have especially suitable habitat  
419 based on the ecological requirements of many of the species modeled. Species that do  
420 not share these ecological requirements will not overlap in distribution. Consequently,  
421 new locations of this type of species will be more likely to occur in the SSC areas of the  
422 efficiency map. For example, *Asplenium scolopendrium*, a fern species that can only  
423 grow on limestone substrate (Oldham & Brinker 2009), was not found at any MSC  
424 locations we searched in 2017. There are contrasting results in the literature concerning  
425 whether or not species with distinct habitat requirements are more easily modeled with  
426 SDMs than generalists (Elith & Burgman 2002, Hernandez et al. 2006, Le Lay et al.  
427 2010, Grenouillet et al. 2011, McCune 2016, Soutan & Safi 2017, Rhoden et al. 2017).  
428 If species with distinct habitats are in fact easily modeled, then their lack of discovery in  
429 our efficiency maps is not a major point of concern because any specialized species of  
430 particular interest can be separately modeled. The methodology presented here focuses  
431 on efficiently finding the most occurrences of rare plant species and not necessarily on

432 finding individual species. If the latter is the desired conservation outcome, an individual  
433 SDM should be used.

434         Of course, our models, like all SDMs, were imperfect. For example, the field  
435 surveys that informed the models likely did not sample the full niche space, and the  
436 AUC of our models may not perfectly reflect model accuracy, in part due to this  
437 measure's effective lowering of species prevalence (Raes & ter Steege, 2007).  
438 However, our results clearly indicate that even such imperfect models can be very good  
439 at efficiently indicating potential survey sites for rare species.

440         Like Williams et al. (2009), we found that many surveyed sites with high  
441 probability of occurrence lacked our rare species, which is likely a result of factors other  
442 than habitat suitability leading to species absence. Dispersal limitation could act as one  
443 of these additional distribution determinants. Suitable habitat may exist outside of where  
444 the species of interest is currently found, but the species' physical inability to spread to  
445 these areas through seeds or spores restricts its distribution to a smaller area. Previous  
446 research has found differences in the amount of predicted suitable habitat when  
447 dispersal is or is not accounted for in plant distribution models, with less habitat  
448 available when dispersal is restricted (Krause et al. 2015). Given that the ability of  
449 plants to disperse is limited and that dispersal can be especially problematic for rare  
450 plant species (Primack and Miao 1992), dispersal limitations should be kept in mind  
451 when creating models for rare plant species. Another limit to plant species real  
452 distributions beyond the abiotic environment could be biotic interactions, including  
453 pollinators (Giannini et al. 2013), pathogens (Bueno de Mesquita et al. 2016), and  
454 competition from other plant species (Meier et al. 2010; Pellissier et al. 2010). Modelers

455 may also choose to include the distributions of one or more interacting species to create  
456 more realistic models.

457

458           Our results did not show a clear difference among the weighting systems  
459 (species S-rank, model accuracy, both, neither) in predicting the presence of at least  
460 one rare plant species using our  $\Delta AIC$  criterion. However, there was a strong  
461 relationship between the efficiency index and the estimated probability of occurrence of  
462 rare species. Thus, although the stacking of individual model outputs was useful for  
463 discovering new rare plant occurrences, the weighting of model outputs by threat level  
464 and model accuracy was unnecessary in this study for the goal of field site survey  
465 prioritization. Dunn et al. (2016) also found that weighting SDMs did not change the  
466 areas highlighted for conservation very much compared to unweighted SDM stacking.  
467 This does not mean that model weighting by either threat level or accuracy should be  
468 completely discounted for future S-SDM analysis. It is possible that a similar weighting  
469 system used in another study area, with a different combination of species, or with more  
470 surveyed cells would have different results.

#### 471 **Acknowledgements**

472 We thank J. Lloren, J. Pon, and C. Raymond for field work assistance. M. Oldham, T.  
473 Smith, and E. Snyder provided plant identification advice. The Natural Heritage  
474 Information Centre of Ontario provided the occurrence records for all species. We also  
475 thank the private landowners who allowed us access to their woodlots, as well as to The  
476 Nature Conservancy of Canada, Ontario Nature, the Province of Ontario, and the

477 University of Waterloo, for granting permits to access protected areas. This research  
478 was funded by the Ontario Ministry of Natural Resources and Forestry's Species at Risk  
479 Stewardship Fund, the Natural Science and Engineering Research Council of Canada  
480 (NSERC) through a Postdoctoral Fellowship to JLM and a Discovery Grant to JRB, and  
481 a Liber Ero fellowship to JLM.

## 482 **Literature Cited**

- 483 Albuquerque F, Beier P (2016) Predicted rarity-weighted richness, a new tool to  
484 prioritize sites for species representation. *Ecology and Evolution* 6:8107-8114.
- 485 Amaral AG, Munhoz CB, Walter BM, Aguirre-Gutiérrez J, Raes N (2017) Richness  
486 pattern and phytogeography of the Cerrado's herb-shrub flora and implications  
487 for conservation. *Journal of Vegetation Science* 28:848-858.
- 488 Bennett JR (2014) Comparison of native and exotic distribution and richness models  
489 across scales reveals essential conservation lessons. *Ecography* 37:120-129.
- 490 Bucklin, D.N., Basille, M., Benscoter, A.M., Brandt, L.A., Mazzotti, F.J., Romanach,  
491 S.S., Speroterra, C., Watling, J.I. (2015) Comparing species distribution models  
492 constructed with different subsets of environmental predictors. *Diversity and*  
493 *Distributions*, 21:23-35.
- 494 Bueno de Mesquita, C. P., King, A. J., Schmidt, S. K., Farrer, E. C., & Suding, K. N.  
495 (2016). Incorporating biotic factors in species distribution modeling: are  
496 interactions with soil microbes important?. *Ecography*, 39(10), 970-980.
- 497 Burnham KP, Anderson DR (2002) Model selection and multi-model inference: a  
498 practical information-theoretic approach, 2nd edition. Springer-Verlag, New York,  
499 USA.
- 500 Calabrese JM, Certain G, Kraan C, Dormann CF (2014) Stacking species distribution  
501 models and adjusting bias by linking them to macroecological models. *Global*  
502 *Ecology and Biogeography* 23:99-112.
- 503 Cord, A. F., Klein, D., Mora, F., & Dech, S. (2014). Comparing the suitability of classified  
504 land cover data and remote sensing variables for modeling distribution patterns  
505 of plants. *Ecological Modelling*, 272: 129-140.
- 506 Crins WJ, Gray PA, Uhlig PWC, Wester MC (2009) The ecosystems of Ontario, part I:  
507 ecozones and ecoregions. Ontario Ministry of Natural Resources, Peterborough,  
508 ON.
- 509 D'Amen M, Dubuis A, Fernandes RF, Pottier J, Pellissier L, Guisan A (2015) Using  
510 species richness and functional traits predictions to constrain assemblage

511 predictions from stacked species distribution models. *Journal of Biogeography*  
512 42:1255-1266.

513 Del Toro, I., Ribbons, R. R., Hayward, J., & Andersen, A. N. (2019). Are stacked  
514 species distribution models accurate at predicting multiple levels of diversity  
515 along a rainfall gradient?. *Austral Ecology*, 44(1), 105-113.

516 Dunn JC, Buchanan GM, Stein RW, Whittingham MJ, McGowan PJ (2016) Optimising  
517 different types of biodiversity coverage of protected areas with a case study  
518 using Himalayan Galliformes. *Biological Conservation* 196:22-30.

519 Dubuis A, Pottier J, Rion V, Pellissier L, Theurillat JP, Guisan A (2011) Predicting  
520 spatial patterns of plant species richness: a comparison of direct macroecological  
521 and species stacking modelling approaches. *Diversity and Distributions* 17:1122-  
522 1131.

523 Elith J, Burgman MA (2002) Predictions and their validation: rare plants in the Central  
524 Highlands, Victoria, Australia. Pages 303-313 in *Predicting species occurrences:*  
525 *issues of accuracy and scale.* J.M. Scott, P.J. Heglund, M.L. Morrison, J.B.  
526 Haufler, M.G. Raphael, W.A. Wall F.B. Samson, editors. Island Press,  
527 Washington, DC.

528 Elith J, Graham CH (2009) Do they? How do they? WHY do they differ? On finding  
529 reasons for differing performances of species distribution models. *Ecography*  
530 32:66-77.

531 Elith J, *et al* (2006) Novel methods improve prediction of species' distributions from  
532 occurrence data. *Ecography* 29:129-151.

533 Elith J, Kearney M, Phillips S (2010) The art of modelling range-shifting species.  
534 *Methods in Ecology and Evolution* 1:330-342.  
535

536 Elith J, Leathwick JR (2009) Species distribution models: ecological explanation and  
537 prediction across space and time. *Annual Review of Ecology, Evolution, and*  
538 *Systematics* 40:677-697.  
539

540 Engler R, Guisan A, Rechsteiner L (2004) An improved approach for predicting the  
541 distribution of rare and endangered species from occurrence and pseudo-  
542 absence data. *Journal of Applied Ecology* 41:263-274.  
543

544 Eskildsen, A., le Roux, P.C., Heikkinen, R.K., Høye, T.T., Kissling, W.D., Pöyry, J.,  
545 Wisz, M.S. and Luoto, M. (2013) Testing species distribution models across  
546 space and time: high latitude butterflies and recent warming. *Global Ecology and*  
547 *Biogeography*, 22:1293-1303.  
548

549 Faber-Langendoen D, Nichols J, Master L, Snow K, Tomaino A, Bittman R,  
550 Hammerson G, Heidel B, Ramsay L, Teucher A, Young B (2012) *NatureServe*  
551 *Conservation Status Assessments: Methodology for Assigning Ranks.*  
552 *NatureServe, Arlington, VA.*

553  
554 Fernandes, R. F., Scherrer, D., & Guisan, A. (2018). How much should one sample to  
555 accurately predict the distribution of species assemblages? A virtual community  
556 approach. *Ecological Informatics*, 48:125-134.  
557  
558 Ferrier S, Guisan A (2006) Spatial modelling of biodiversity at the community level.  
559 *Journal of Applied Ecology* 43:393-404.  
560  
561 Fielding AH, Bell JF (1997) A review of methods for the assessment of prediction errors  
562 in conservation presence/absence models. *Environmental Conservation* 24:38–  
563 49.  
564  
565 Giannini, T. C., Chapman, D. S., Saraiva, A. M., Alves-dos-Santos, I., & Biesmeijer, J.  
566 C. (2013). Improving species distribution models using biotic interactions: a case  
567 study of parasites, pollinators and plants. *Ecography*, 36(6), 649-656.  
568  
569 Gogol-Prokurat M (2011) Predicting habitat suitability for rare plants at local spatial  
570 scales using a species distribution model. *Ecological Applications* 21:33-47.  
571  
572 Graham, CH, Ferrier S, Huettman F, Moritz C, Peterson AT (2004) New  
573 developments in museum-based informatics and applications in biodiversity  
574 analysis. *Trends in Ecology & Evolution* 19:497-503.  
575  
576 Grenouillet G, Buisson L, Casajus N, Lek S (2011) Ensemble modelling of species  
577 distribution: the effects of geographical and environmental ranges. *Ecography*  
578 34:9-17.  
579  
580 Guisan A, Rahbek C (2011) SESAM—a new framework integrating macroecological  
581 and species distribution models for predicting spatio-temporal patterns of species  
582 assemblages. *Journal of Biogeography* 38:1433-1444.  
583  
584 Guisan A *et al* (2013) Predicting species distributions for conservation decisions.  
585 *Ecology Letters* 16:1424-1435.  
586  
587 Guisan A, Theurillat, JP (2000) Equilibrium modeling of alpine plant distribution: how far  
588 can we go?. *Phytocoenologia* 30:353-384.  
589  
590 Guisan A, Zimmermann NE (2000) Predictive habitat distribution models in  
591 ecology. *Ecological Modelling* 135:147-186.  
592  
593 Guisan A, Zimmermann N, Elith J, Graham C, Phillips S, Peterson A (2007) What  
594 matters for predicting spatial distributions of tree occurrences: techniques, data,  
595 or species' characteristics. *Ecological Monographs* 77:615–630.  
596  
597 Hernandez PA, Graham CH, Master LL, Albert DL (2006) The effect of sample size and  
598 species characteristics on performance of different species distribution modeling  
599 methods. *Ecography* 29:773–785

596 R Core Team (2016) R: a language and environment for statistical computing. R  
597 Foundation for Statistical Computing, Vienna

598 Hijmans RJ & van Etten J (2017). raster: Geographic analysis and modeling with raster  
599 data. <https://CRAN.R-project.org/package=raster>

600 Krause, C. M., Cobb, N. S., & Pennington, D. D. (2015). Range shifts under future  
601 scenarios of climate change: dispersal ability matters for Colorado Plateau  
602 endemic plants. *Natural Areas Journal*, 35(3), 428-438.

603 Koch R, Almeida-Cortez JS, Kleinschmit B (2017) Revealing areas of high nature  
604 conservation importance in a seasonally dry tropical forest in Brazil: Combination  
605 of modelled plant diversity hot spots and threat patterns. *Journal for Nature  
606 Conservation* 35:24-39.

607 Le Lay G, Engler R, Franc E, Guisan A (2010) Prospective sampling based on model  
608 ensembles improves the detection of rare species. *Ecography* 33:1015-1027.  
609

610 Lindenmayer DB, Piggott MP, Wintle BA (2013) Counting the books while the library  
611 burns: why conservation monitoring programs need a plan for action. *Frontiers in  
612 Ecology and the Environment* 11:549-555.

613 Liu C, Newell G, White M (2016) On the selection of thresholds for predicting  
614 species occurrence with presence-only data. *Ecology and Evolution* 6:337-  
615 348.

616 Loiselle BA, Howell CA, Graham, CH, Goerck JM, Brooks T, Smith KG, Williams PH  
617 (2003) Avoiding pitfalls of using species distribution models in conservation  
618 planning. *Conservation Biology* 17:1591-1600.

619 Luoto, M., Pöyry, J., Heikkinen, R. K., & Saarinen, K. (2005). Uncertainty of bioclimate  
620 envelope models based on the geographical distribution of species. *Global  
621 Ecology and Biogeography*, 14: 575-584.

622 Luoto, M., Virkkala, R., & Heikkinen, R. K. (2007). The role of land cover in bioclimatic  
623 models depends on spatial resolution. *Global Ecology and Biogeography*, 16: 34-  
624 42.

625 MacDougall A, Loo J (2002) Land use history, plant rarity, and protected area adequacy  
626 in an intensively managed forest landscape. *Journal for Nature Conservation*  
627 10:171-183.

628 McCune JL (2016) Species distribution models predict rare species occurrences  
629 despite significant effects of landscape context. *Journal of Applied Ecology*  
630 53:1871-1879.

631 McCune JL, Van Natto A, MacDougall AS (2017) The efficacy of protected areas and  
632 private land for plant conservation in a fragmented landscape. *Landscape  
633 Ecology* 32:871-882.

- 634 McKenney DW, Pedlar JH, Lawrence K, Papadopol P, Campbell K (2015) Hardiness  
635 zones and bioclimatic modelling of plant species distributions in North America.  
636 *Acta Horticulturae*. 1085, 139-148
- 637 Meier, E.S., Kienast, F., Pearman, P.B., Svenning, J.C., Thuiller, W., Araújo, M.B.,  
638 Guisan, A. and Zimmermann, N.E. (2010). Biotic and abiotic variables show little  
639 redundancy in explaining tree species distributions. *Ecography*, 33(6), 1038-  
640 1048.
- 641 Merow C, Smith MJ, Silander JA (2013) A practical guide to MaxEnt for modeling  
642 species' distributions: what it does, and why inputs and settings matter.  
643 *Ecography* 36:1058-1069.
- 644 Miličić M, Vujić A, Jurca T, Cardoso P (2017) Designating conservation priorities for  
645 Southeast European hoverflies (Diptera: Syrphidae) based on species  
646 distribution models and species vulnerability. *Insect Conservation and Diversity*  
647 10:354-366.
- 648 Moudrý V, Šimová P (2012) Influence of positional accuracy, sample size and scale on  
649 modelling species distributions: a review. *International Journal of Geographical*  
650 *Information Science* 26:2083-2095.
- 651 Newbold T, Gilbert F, Zalut S, El-Gabbas A, Reader T (2009) Climate-based models of  
652 spatial patterns of species richness in Egypt's butterfly and mammal fauna.  
653 *Journal of Biogeography* 36:2085-2095.
- 654 Oldham MJ, Brinker SR (2009) *Rare Vascular Plants of Ontario*, 4<sup>th</sup> edition. Natural  
655 Heritage Information Centre, Ontario Ministry of Natural Resources.  
656 Peterborough, ON.
- 657 Oldham MJ (2017) *List of the Vascular Plants of Ontario's Carolinian Zone*  
658 (Ecoregion 7E). Carolinian Canada and Ontario Ministry of Natural Resources  
659 and Forestry. Peterborough, ON.
- 660 Parviainen M, Marmion M, Luoto M, Thuiller W, Heikkinen RK (2009) Using summed  
661 individual species models and state-of-the-art modelling techniques to identify  
662 threatened plant species hotspots. *Biological Conservation* 142:2501-2509.
- 663 Pearce, J. & Ferrier, S (2000) Evaluating the predictive performance of habitat models  
664 developed using logistic regression. *Ecological Modelling*, 133, 225 – 245.
- 665 Pearson RG, Raxworthy CJ, Nakamura M, Peterson AT (2007) Predicting species  
666 distributions from small numbers of occurrence records: a test case using cryptic  
667 geckos in Madagascar. *Journal of Biogeography* 34:102–117
- 668 Pellissier, L., Anne Bråthen, K., Pottier, J., Randin, C.F., Vittoz, P., Dubuis, A., Yoccoz,  
669 N.G., Alm, T., Zimmermann, N.E. and Guisan, A. Species distribution models  
670 reveal apparent competitive and facilitative effects of a dominant species on the  
671 distribution of tundra plants. *Ecography*, 33(6), 1004-1014.

672 Peterson AT, Soberon, J, Pearson RG, Anderson RP, Martínez-Meyer E, Nakamura M,  
673 Araujo MB (2011) Ecological niches and geographic distributions. Princeton, NJ:  
674 Princeton University Press.

675 Phillips SJ, Anderson RP, Schapire RE (2006) Maximum entropy modeling of  
676 species geographic distributions. *Ecological Modelling* 190:231–259.

677 Pouteau, R., Bayle, É., Blanchard, É., Birnbaum, P., Cassan, J.J., Hequet, V., Ibanez,  
678 T. and Vandrot, H. (2015) Accounting for the indirect area effect in stacked species  
679 distribution models to map species richness in a montane biodiversity hotspot. *Diversity  
680 and Distributions* 21:1329-1338.

681

682 Primack, R. B., & Miao, S. L. (1992). Dispersal can limit local plant distribution.  
683 *Conservation Biology*, 6(4), 513-519.

684 Raes, N., & ter Steege, H. (2007) A null-model for significance testing of presence-only  
685 species distribution models. *Ecography*, 30: 727-736.

686 Rebelo H, Jones G (2010) Ground validation of presence-only modelling with rare  
687 species: a case study on barbastelles *Barbastella barbastellus* (Chiroptera:  
688 *Vespertilionidae*). *Journal of Applied Ecology* 47:410-420.

689 Rhoden CM., Peterman WE, Taylor CA (2017) Maxent-directed field surveys identify  
690 new populations of narrowly endemic habitat specialists. *PeerJ* 5:e3632. DOI:  
691 10.7717/peerj.3632

692 SARA (Species at Risk Act) (2002) Bill C-5, an Act Respecting the Protection of Wildlife  
693 Species at Risk in Canada. Government of Canada, Ottawa, Ontario.

694 Segurado P, Araujo MB (2004) An evaluation of methods for modelling species  
695 distributions. *Journal of Biogeography* 31:1555-1568.

696 Soutan A, Safi K (2017) The interplay of various sources of noise on reliability of  
697 species distribution models hinges on ecological specialisation. *PIOS ONE*  
698 12:e0187906. DOI: 10.1371/journal.pone.0187906

699

700 Swets JA (1988) Measuring the accuracy of diagnostic systems. *Science*  
701 240:1285–1293.

702

703 Syphard AD, Franklin J (2010) Species traits affect the performance of species  
704 distribution models for plants in southern California. *Journal of Vegetation  
705 Science* 21:177-189.

706 Thuiller W (2004) Patterns and uncertainties of species' range shifts under climate  
707 change. *Global Change Biology* 10:2020-2027.

708 Thuiller W, Lavorel S, Araújo MB, Sykes MT, Prentice IC (2005) Climate change threats  
709 to plant diversity in Europe. *Proceedings of the National Academy of Sciences of  
710 the United States of America* 102:8245-8250.

711 Tukiainen H, Bailey JJ, Field R, Kangas K, Hjort J (2017) Combining geodiversity with  
712 climate and topography to account for threatened species richness. *Conservation*  
713 *Biology* 31:364-375.

714 van Proosdij AS, Sosef MS, Wieringa JJ, Raes N (2016) Minimum required number of  
715 specimen records to develop accurate species distribution models. *Ecography*  
716 39:542-552.

717 Vaughan IP, & Ormerod, SJ (2005) The continuing challenges of testing species  
718 distribution models. *Journal of Applied Ecology*, 42:720-730.

719 Williams JN, Seo C, Thorne J, Nelson JK, Erwin S, O'Brien JM, Schwartz MW (2009)  
720 Using species distribution models to predict new occurrences for rare plants.  
721 *Diversity and Distributions* 15:565-576.

722 Wilson, J. W., Sexton, J. O., Jobe, R. T., & Haddad, N. M. (2013). The relative  
723 contribution of terrain, land cover, and vegetation structure indices to species  
724 distribution models. *Biological Conservation*, 164, 170-176.

725 Yu F, Skidmore AK, Wang T, Huang J, Ma K, Groen TA (2017) Rhododendron diversity  
726 patterns and priority conservation areas in China. *Diversity and Distributions*  
727 23:1143-1156.

728 Zimmermann NE, Edwards TC, Moisen GG, Frescino TS, Blackard JA (2007) Remote  
729 sensing-based predictors improve distribution models of rare, early successional  
730 and broadleaf tree species in Utah. *Journal of Applied Ecology* 44:1057-1067.

731 **Tables**

732 **Table 1:** Model information for each of the 27 species tested, including the 22 species  
733 included in the S-SDM efficiency map.

734

Species	Number of Records	AUC	S-rank	Total Weight*
<i>Aplectrum hyemale</i>	5	0.734	S2	1.468
<i>Arisaema dracontium</i> **	73	0.595	S3	-
<i>Asclepias quadrifolia</i>	7	0.999	S1	2.997
<i>Asimina triloba</i>	43	0.779	S3	0.779
<i>Asplenium scolopendrium</i>	144	0.981	S3	0.981
<i>Castanea dentata</i>	153	0.813	S2	1.626
<i>Celtis tenuifolia</i>	73	0.968	S2	1.936
<i>Chimaphila maculata</i>	15	0.983	S1	2.949
<i>Corallorhiza odontorhiza</i>	4	0.913	S2	1.826
<i>Cornus florida</i>	295	0.775	S2	1.55
<i>Cypripedium arietinum</i>	65	0.860	S3	0.860
<i>Enemion biternatum</i>	14	0.862	S2	1.724
<i>Erigenia bulbosa</i> **	8	0.453	S2S3	-

<i>Frasera caroliniensis</i>	30	0.882	S2	1.764
<i>Fraxinus quadrangulata</i>	46	0.865	S3	0.865
<i>Heuchera americana</i>	19	0.907	S2	1.814
<i>Hydrastis canadensis</i>	44	0.826	S2	1.652
<i>Juglans cinerea</i> **	1594	0.467	S2	-
<i>Liparis liliifolia</i>	16	0.971	S2	1.942
<i>Lithospermum latifolium</i>	11	0.664	S3	0.664
<i>Magnolia acuminata</i>	58	0.847	S2	1.694
<i>Mertensia virginica</i>	6	0.828	S2	1.656
<i>Morus rubra</i> **	42	0.780	S2	-
<i>Phegopteris hexagonoptera</i> **	38	0.632	S3	-
<i>Stylophorum diphyllum</i>	6	0.959	S1	2.877
<i>Trillium flexipes</i>	4	0.967	S1	2.901
<i>Uvularia perfoliata</i>	9	0.938	S1	2.814

735

736 \*Includes both weight for model accuracy and species conservation status

737 \*\*Species not included in the S-SDM due to low independent AUC and/or GLM that  
738 does not predict probability of occurrence better than an intercept-only model.

739

740

741 **Table 2:** Results of the generalized linear models predicting probability of at least one  
742 species of conservation concern based on S-SDM score for each of the different  
743 weighting procedures.

744

Weighting	AIC	Null Deviance	Residual Deviance	% Deviance Explained
None	79.155	81.686	75.155	8.0
Model Accuracy	78.863	81.686	74.863	8.4
Species S-rank	79.778	81.686	75.778	7.2
Both	79.545	81.686	75.545	7.5

745

746

747 Figure Captions:

748

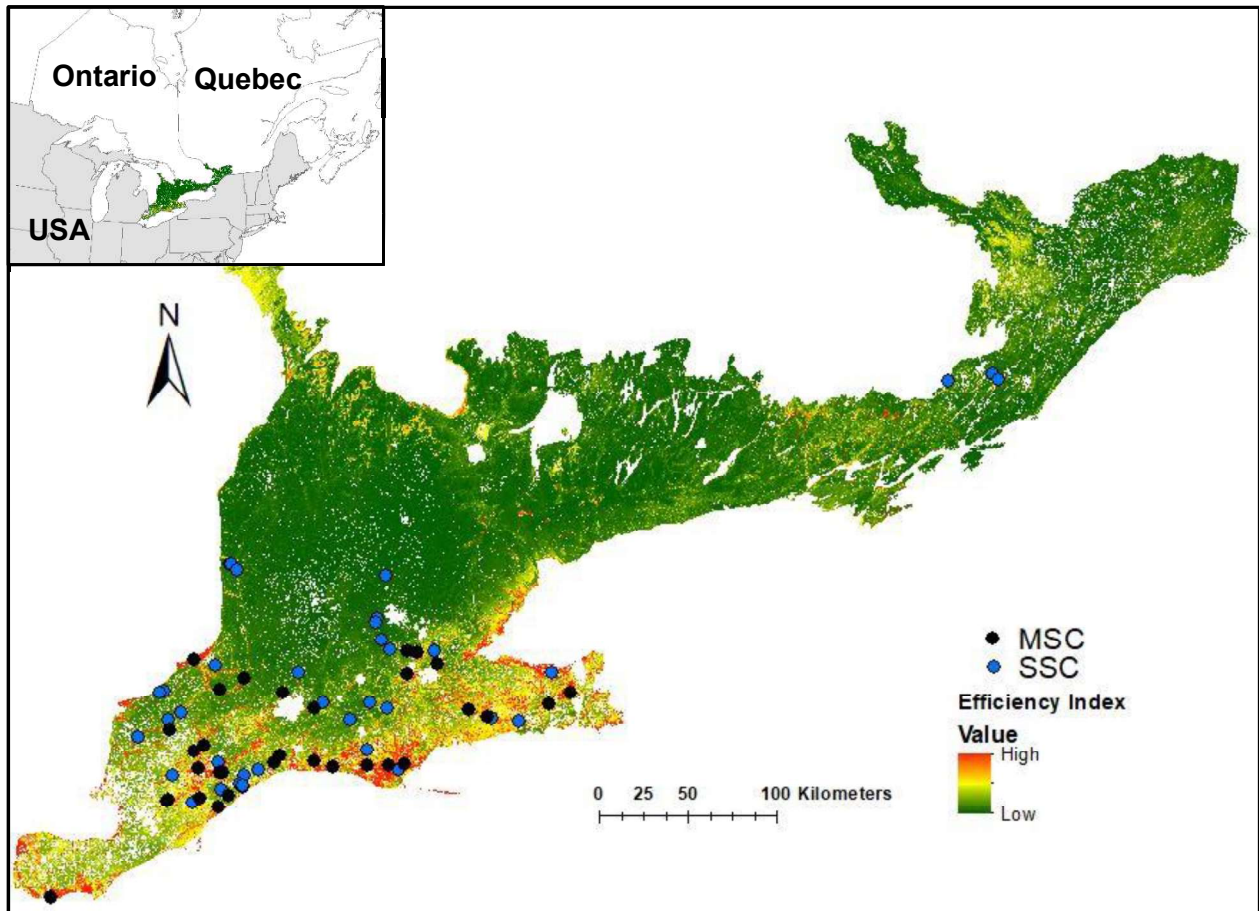
749 Figure 1: Study area showing the range of efficiency index values based on weighting  
750 individual model outputs by species rarity and model accuracy with the multi-species  
751 cell (MSC) and single species cell (SSC) sites surveyed in 2017 overlaid.

752 Figure 2: Flowchart showing progression of steps taken to attain efficiency maps from  
753 Maxent SDMs.

754 Figure 3: A) The percent of multi-species cell (MSC) and single species cell (SSC) plots  
755 that had at least one rare plant species discovered, either including or excluding  
756 incidental species discoveries (species which were not modeled) and B) Visualization of  
757 logistic regression model showing estimated probability of presence of at least rare  
758 plant species across efficiency index values of the S-SDM weighted by both rarity and  
759 accuracy with 95% confidence intervals.

760

761



762

763

764 Figure 1: Study area showing the range of efficiency index values based on weighting  
765 individual model outputs by species rarity and model accuracy with the multi-species  
766 cell (MSC) and single species cell (SSC) sites surveyed in 2017 overlaid.

767

768

769

770

771

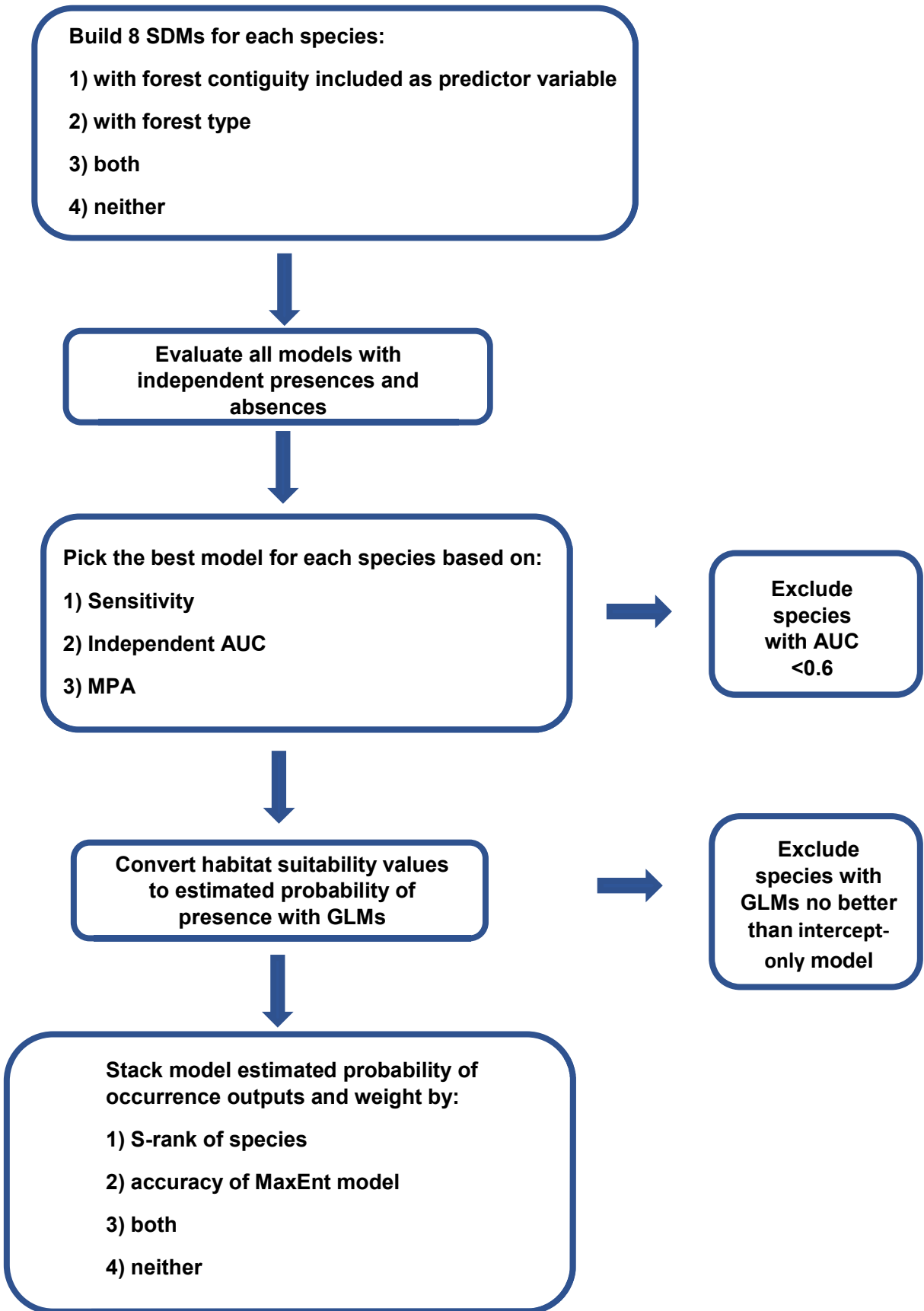
772

773

774

775

776  
777  
778  
779  
780  
781  
782  
783  
784  
785  
786  
787  
788  
789  
790  
791  
792  
793  
794  
795  
796  
797  
798  
799  
800  
801  
802  
803  
804



805 Figure 2: Flowchart showing progression of steps taken to attain efficiency maps from  
806 Maxent SDMs.

807

808

809

810

811

812

813

814

815

816

817

818

819

820

821

822

823

824

825

826

827

828

829

830

831

832

833

834  
835  
836  
837  
838  
839  
840  
841  
842  
843  
844  
845  
846  
847  
848  
849  
850  
851  
852  
853  
854  
855

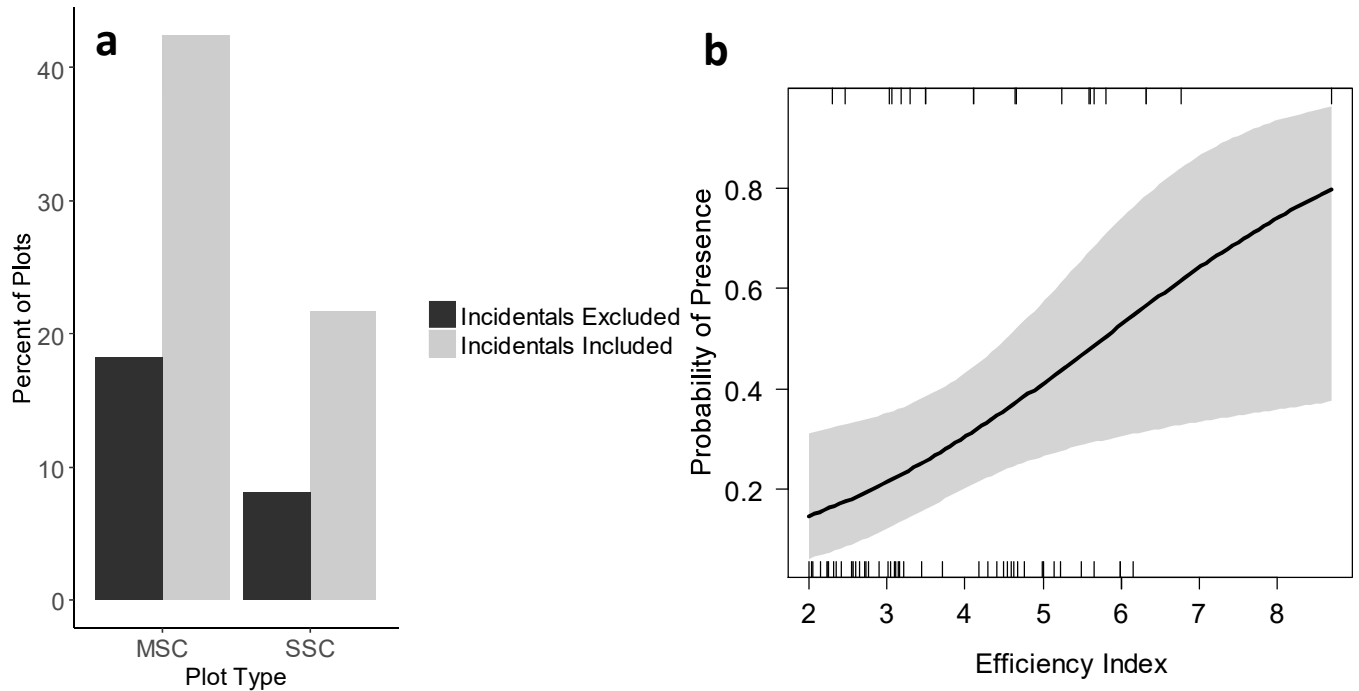


Figure 3: A) The percent of multi-species cell (MSC) and single species cell (SSC) plots that had at least one plant species of conservation concern discovered, either including or excluding incidental species discoveries (species which were not modeled) and B) Visualization of logistic regression model showing estimated probability of presence of at least one rare plant species across efficiency index values of the S-SDM weighted by both rarity and accuracy with 95% confidence intervals.